

Comparing global link arrangements for Dragonfly networks

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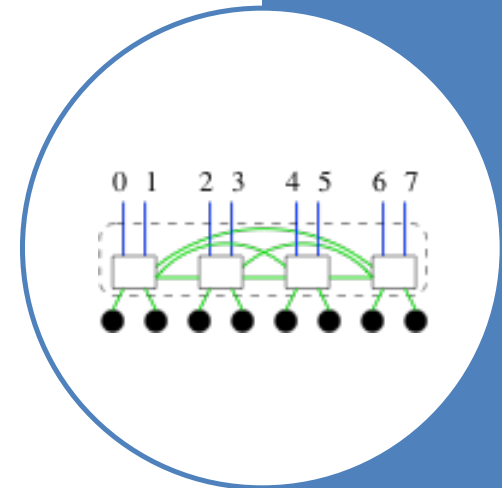
Agenda

- Choice global link arrangement can change the achievable network performance.
 - Absolute
 - Relative
 - Circulant-based
- Global link arrangement's impact on regularity of task mapping



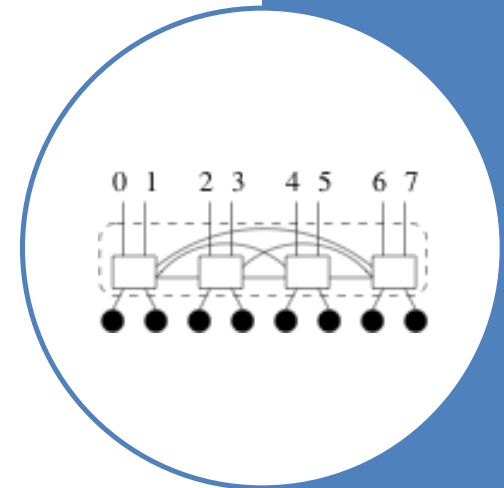
Dragonfly

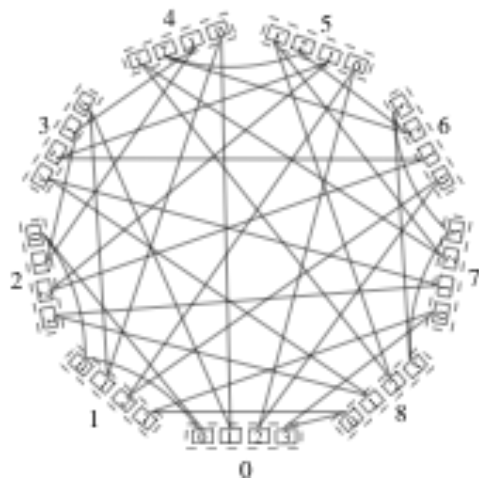
- Hierarchical architecture to exploit high-radix switches and optical links
 - Nodes attached to switches
 - Switches form groups
 - Group members connected w/ local edge
 - Each pair of groups connected w/ global edge



Dragonfly parameters

- p = number of nodes connected to a switch
- a = number of switches in a group
- h = number of global links on a switch
- Number of groups $g = ah+1$

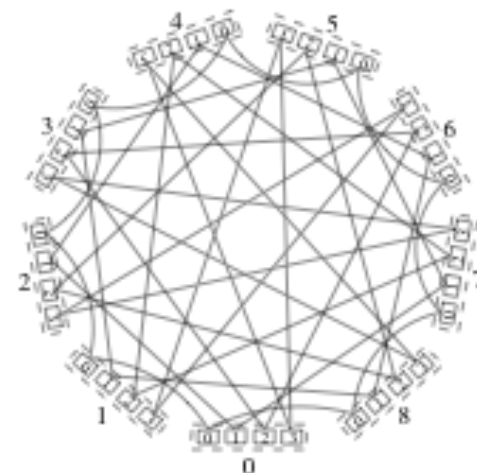




Absolute arrangement



Relative arrangement



Circulant-based arrangement

Three distinct global link
arrangements

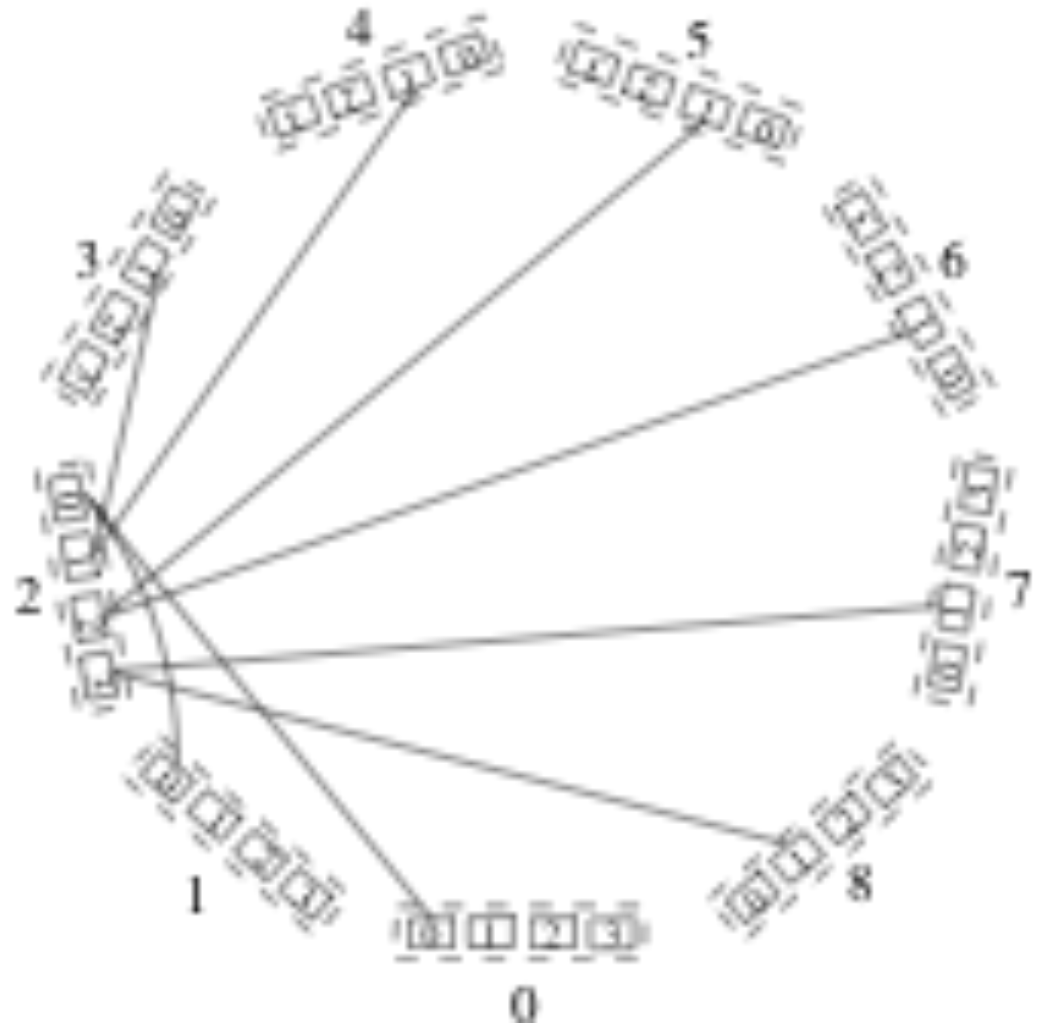


Absolute arrangement

Port k connects to group k
(except skip own group)

Equivalently, port k of group i
connects to

group k if $k < i$
group $k+1$ if $k \geq i$



Relative arrangement

Port k connects $(k+1)^{\text{st}}$ group

Equivalently, port k of group i connects to group $(i+k+1) \bmod g$



Circulant-based arrangement

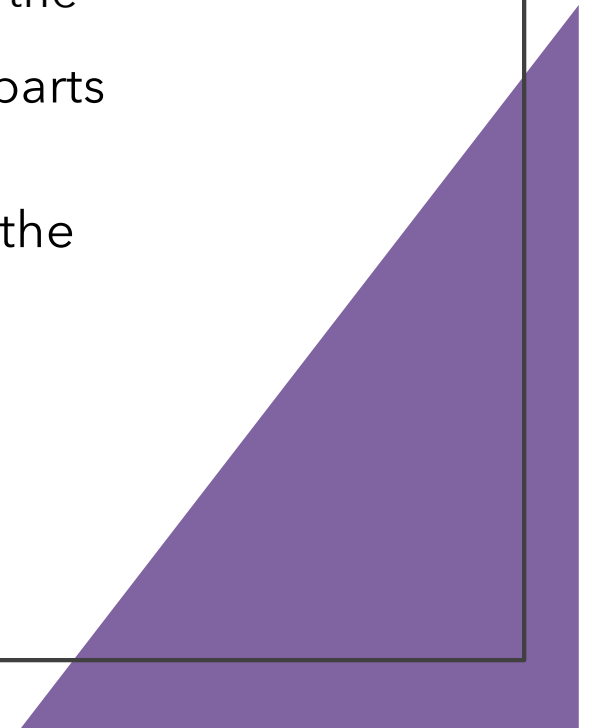
Port 0 connects to next group
Port 1 connects to previous group
Port 2 connects to group 2 ahead
Port 3 connects to group 2 behind
...

Equivalently, port k of group i
connects to group
 $(i+k/2+1) \bmod g$ if k is even
 $(i-k/2-1) \bmod g$ if k is odd



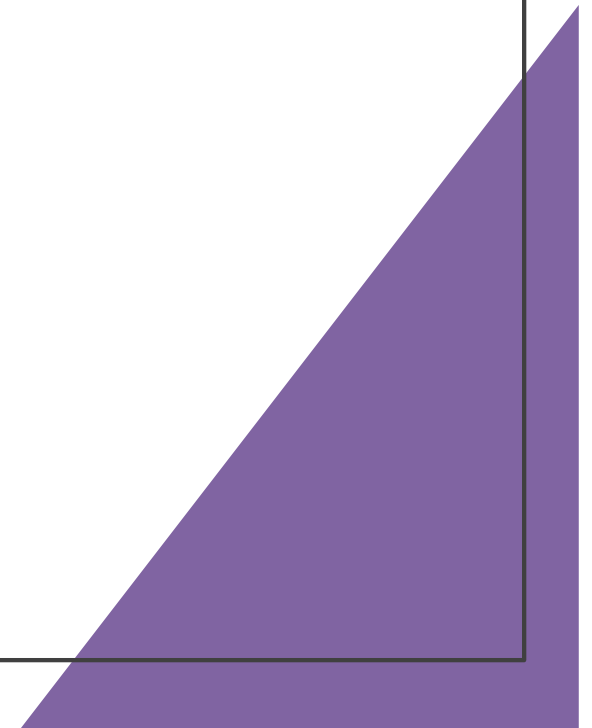
Bisection bandwidth

- Bandwidth varies linearly with n , with the rate depending on the number of global links crossing the cut
- Minimum bandwidth between two equal-sized parts of the system
 - Bandwidth for a particular bisection is the number of edges crossing from one part to the other
 - Minimize this over all bisections
- Tries to measure worst-case communication bottleneck in a large computation

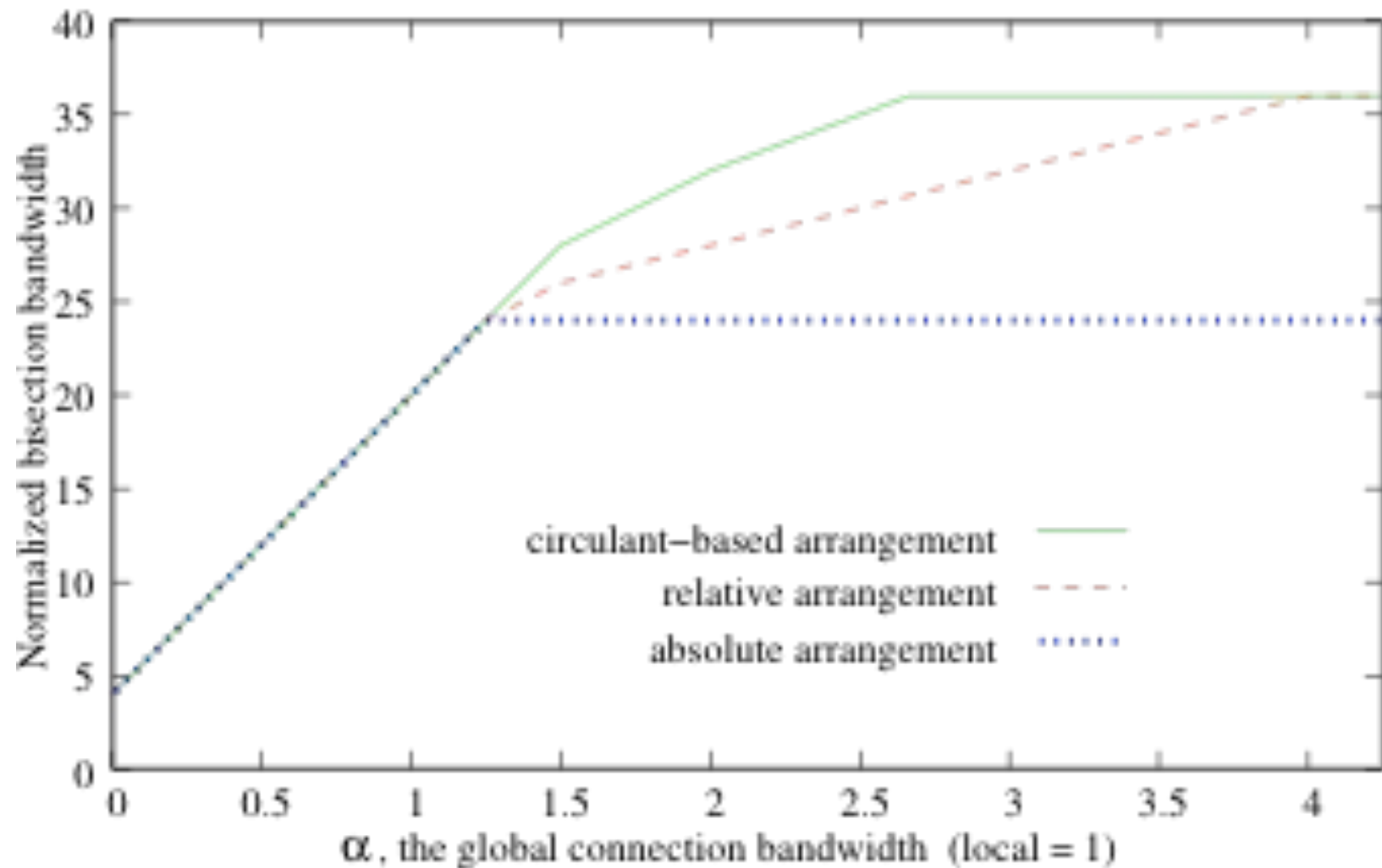


Initial exploration

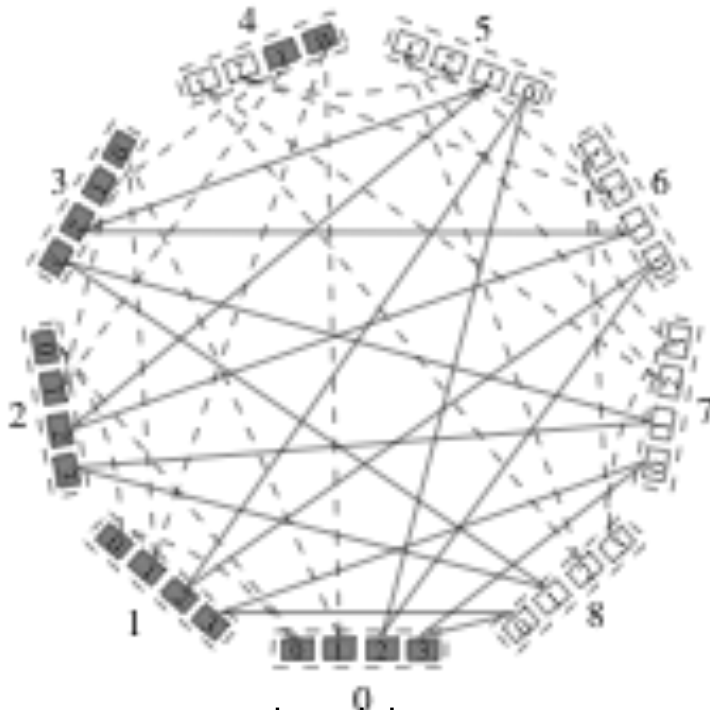
- Small Dragonfly system
 - (p,4,2): 4 switches per group
 - 2 global links per switch
 - Has 36 switches
- Treat types of edges separately
 - local edges have bandwidth 1
 - global edges have bandwidth α



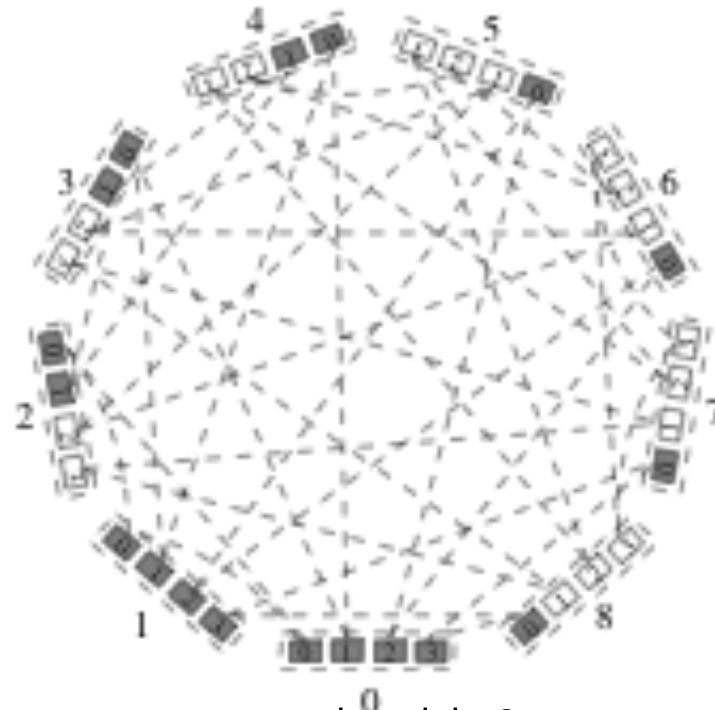
Bisection bandwidth as function of α



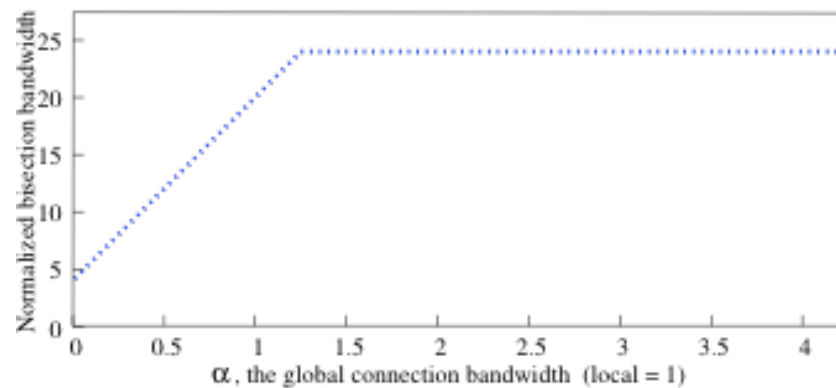
Min-bandwidth cuts for absolute arrangement



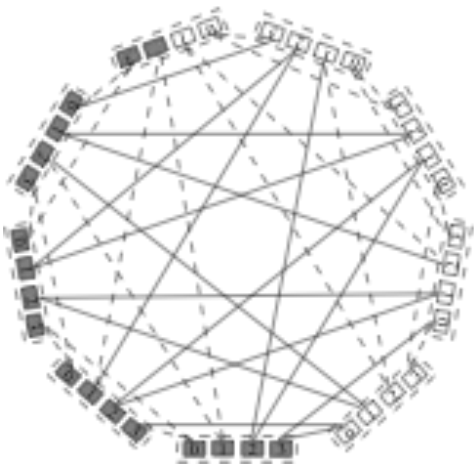
Bandwidth $4 + 16\alpha$



Bandwidth 24



Min-bandwidth cuts for relative arrangement



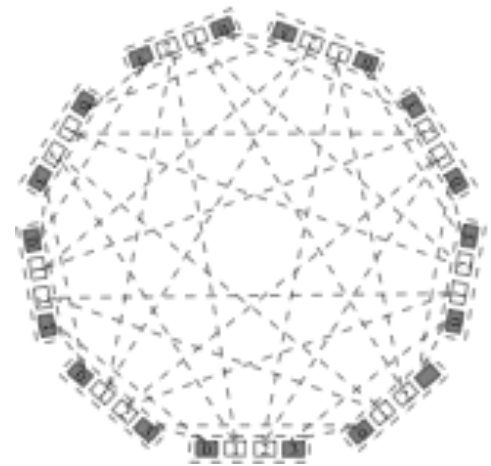
bandwidth $4 + 16\alpha$



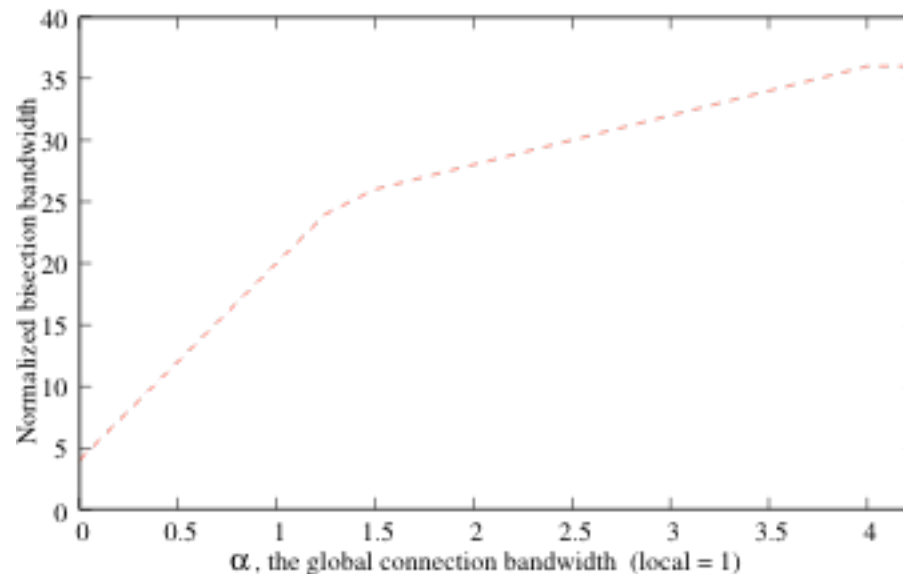
bandwidth $14 + 8\alpha$



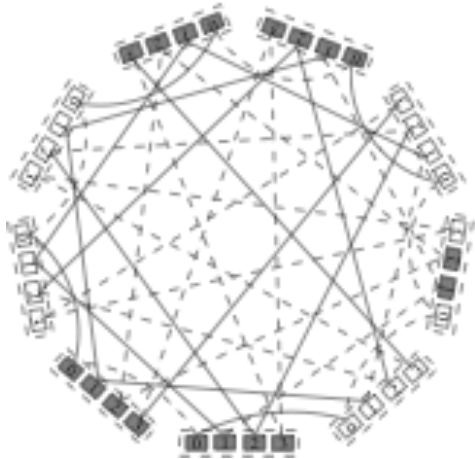
bandwidth $20 + 4\alpha$



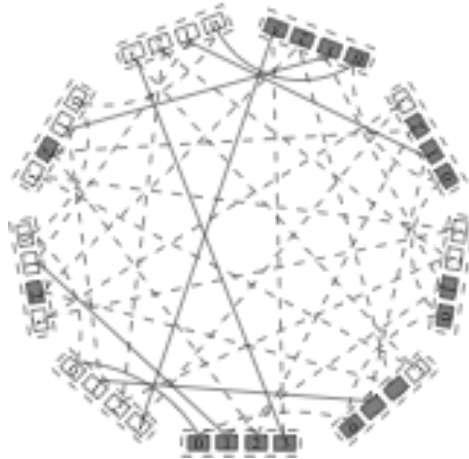
bandwidth 36



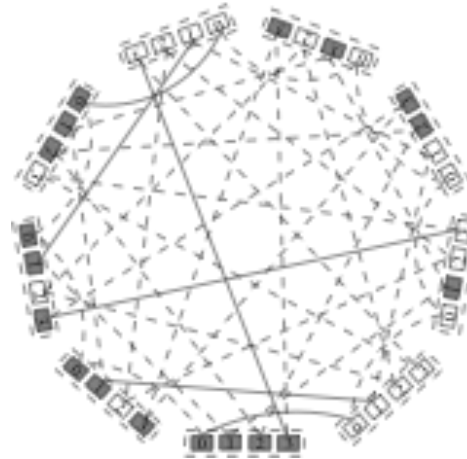
Min-bandwidth cuts for circulant-based arrangement



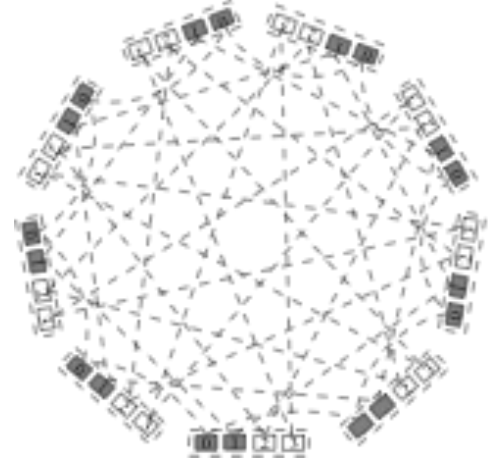
bandwidth $4 + 16\alpha$



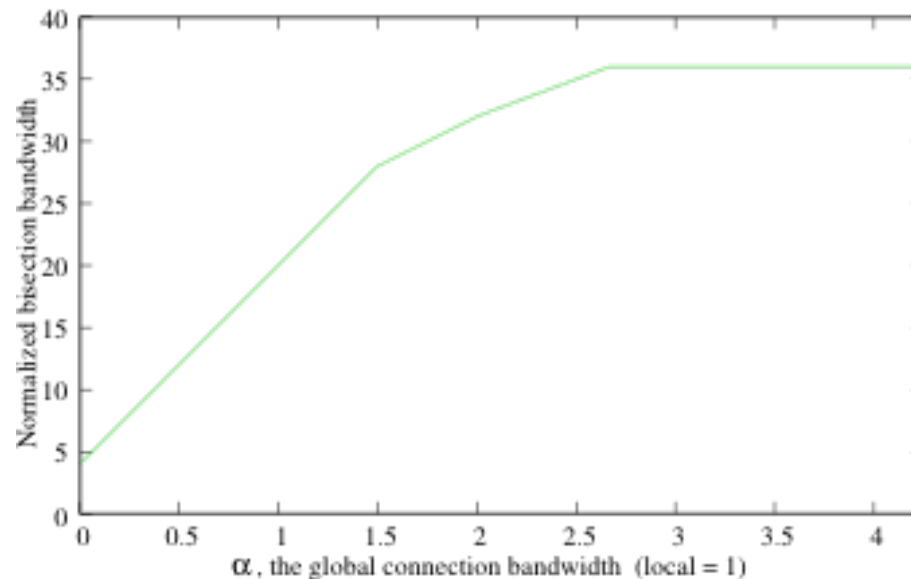
bandwidth $16 + 8\alpha$



bandwidth $20 + 6\alpha$

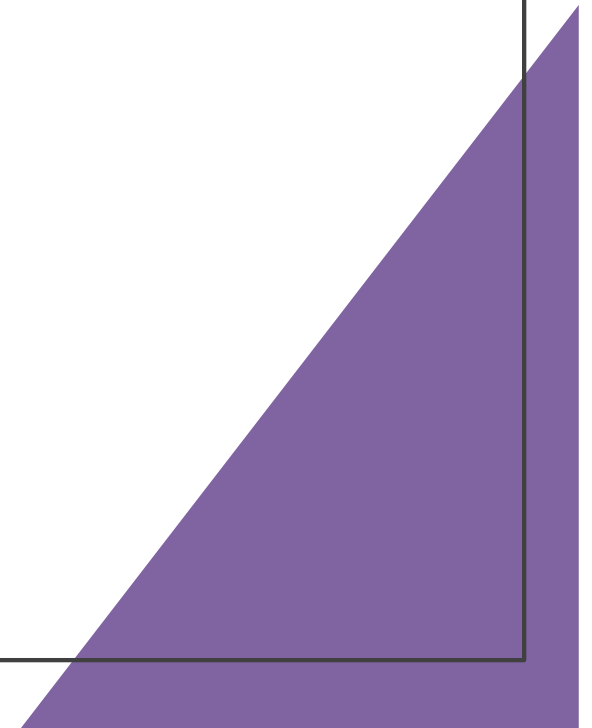


bandwidth 36



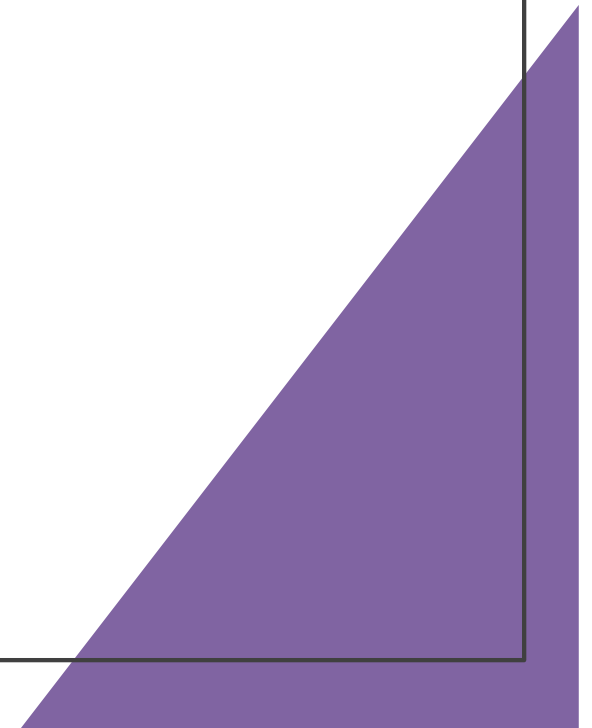
Observations from (p,4,2)

- In terms of bisection bandwidth:
Absolute $\leq$ Relative $\leq$ Circulant-based
- For all three arrangements, maximum bisection bandwidth is bounded



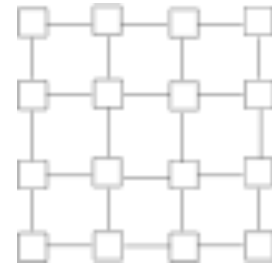
When bisection bandwidth is bounded

- Circulant: a is even
 - $(a/2)^2 g$
- Relative: a is a multiple of 4
 - $(a/2)^2 g$
- Absolute: a is a multiple of 4
 - $\theta(1)$



Task mapping

- Hotspots can still occur
- Assignment of a job's tasks to the processing elements assigned to that job
- Quality task mapping improves application performance by improving bandwidth utilization
- Good mappings are possible under each, the relative arrangement allows mappings with a regularity that will simplify code and improve generalizability



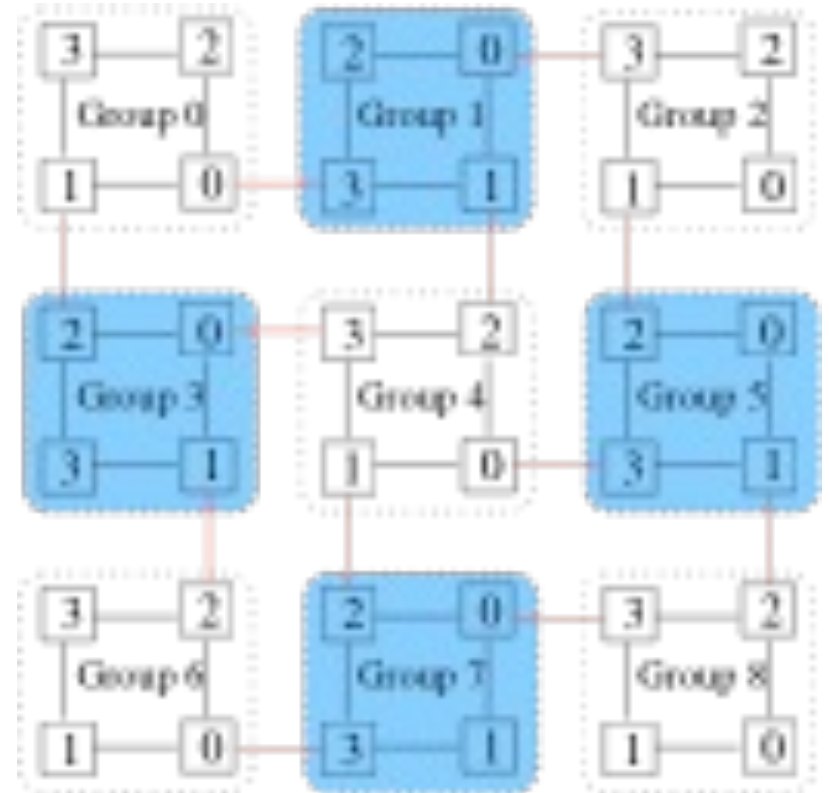
Criteria for good mapping

Communication in phases such that:

1. Messages distributed evenly on links
2. All paths in a phase have same length

Phases for this mapping:

- Neighbors w/ local links
- Neighbors directly connected by global link
- Neighbors with multi-hop path



Final Thoughts

- On small graph, for bisection bandwidth:
Absolute $\leq$ Relative $\leq$ Circulant-based
- On large graphs, Circulant-based is most often bounded, then Absolute, then Relative
- For mapping stencils, Relative gives much more regular mappings

Thank You

